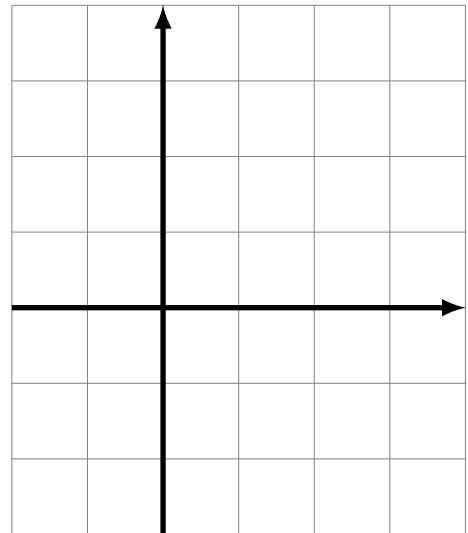


Cases when a solution of a linear program may not exist:

**Infeasibility:** There are no feasible solutions.

**Example.** Maximize  $z = 2x_1 + x_2$  subject to

$$\begin{aligned}x_1 + x_2 &\leq 1 \\ -x_1 + x_2 &\leq -3 \\ x_1, x_2 &\geq 0\end{aligned}$$



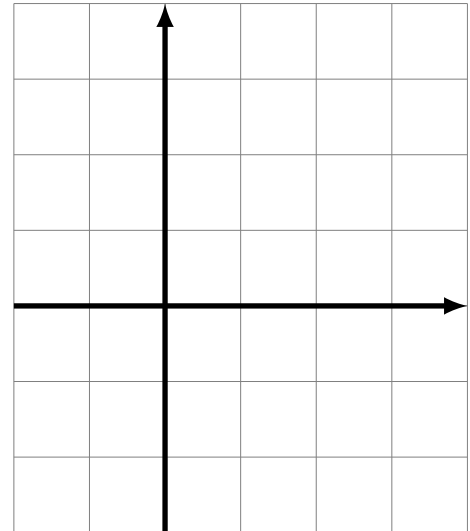
**Unboundedness:** The objective function has no minimum (or maximum) in the feasible region.

**Example.** Maximize  $z = x_1$  subject to

$$x_1 - \frac{2}{3}x_2 \leq 2$$

$$x_1 + x_2 \geq 1$$

$$x_1, x_2 \geq 0$$



**Note.** Even when the feasible region is unbounded the objective function may have a maximum or a minimum in this region.